# Table of Contents

SECTION 1	Introduction	1-1
SECTION 2	Background	2-1
SECTION 3	Direct Table Look-Up 3.1 Integer Delta Implementation 3.2 Real Delta Implementation 3.3 Harmonic Distortion	3-1 3-5 3-10
SECTION 4	Table Look-Up with Linear Interpolation 4.1 Harmonic Distortion	4-1 4-8
APPENDIX A	Computation of Total Harmonic Distortion (THD)	A-1
APPENDIX B	The Sine Table	B-1
FFERENCES	Refere	nce-1

MOTOROLA iii

# Illustrations

Figure 3-1	Integer Delta	3-2
Figure 3-2	"SINWGID" Routine	3-3
Figure 3-3	"SINWGID" Memory Map	3-3
Figure 3-4	Real Data Without Interpolation	3-5
Figure 3-5	"SINWGRD" Routine	3-6
Figure 3-6	"SINWGRD" Memory Map	3-7
Figure 3-7	"SINWGRD" Data ALU Programmer's Model	3-7
Figure 4-1	Real Delta Interpolation	4-2
Figure 4-2	"SINWGLI" Flow Diagram	4-3
Figure 4-3	"SINWGLI" Routine	4-5
Figure 4-4	"SINWGLI" Memory Map	4-6
Figure 4-5	"SINWGLI" Data ALU Programmer's Model	4-7
Figure A-1	VAX VMS FORTRAN Source Code for THD Computation	A-5

MOTOROLA v

# List of Tables

Table 2-1	Sine-Wave Table Values	2-1
Table 3-1	Total Harmonic Distortion — Integer Delta	3-11
Table 3-2	Total Harmonic Distortion — Real Delta	3-12
Table 4-1	Total Harmonic Distortion — Real Delta	4-8
Table A-1	Single Precision Accuracy	A-4
Table A-2	Double Precision Accuracy	A-4
Table B-1	The Sine Table	B-1

MOTOROLA vii

#### **SECTION 1**

#### Introduction

"This document describes three table look-up methods for sine-wave generation . . ." **S**ine-wave generators are used in communications and control applications (1,2). With the introduction of high-speed high-precision digital signal processors, stable and low distortion sine waves of any frequency can be produced digitally using some form of table look-up with interpolation to reduce distortion (3,4,5). This document describes three table look-up methods for sine-wave generation and provides the Total Harmonic Distortion (THD) performance and Maximum Synthesizable Frequency (MSF) for each case.

A routine for synthesizing sine waves having frequencies limited to integer multiples of the Fundamental Table Frequency (FTF) is described in **Section 3.1**. The MSF is highest using this approach. In **Section 3.2** a routine using only direct table look-up for synthesizing sine waves having frequencies which are fractional multiples of the FTF is described. This approach can be used to synthesize sine waves with frequencies which are not integer multiples of the FTF but they have substantially higher THD. A routine for synthesizing sine waves using table look-up with interpolation is described in **Section 4**. Sine waves with frequencies which are not limited to multiples of the FTF and yet have low THD are possibly using this synthesis approach.

#### **SECTION 2**

## Background

"The maximum value delta can assume is N/2 since at least two samples per cycle are required to synthesize a sine wave without aliasing."

The values used for approximating a sine wave are stored in a table in memory as follows:

Table 2-1 Sine-Wave Table Values										
i=N-1	sin[(N-1) • 360/N]									
	•									
	•									
i→	sin[(i) • 360/N]									
	•									
	•									
	sin[(2) • 360/N]									
	sin[(1) • 360/N]									
BASE ADDRESS (I=0)	sin[(0) • 360/N]									

where:

N = the table length

 $i = the index into the table; 0 \le i \le N - 1$ 

sin[i•360/N] = the value stored at the jth location in the table. i • 360/N is the angle,

in degrees, for which the sine function is calculated. Throughout the remainder of this document, the abbreviation S[i] will be used to rep-

resent this function.

Note that the length of the table can be traded off against software in that, except for the sign, only one quarter of the table values are unique. The frequency of the digital sine wave generated depends upon the time interval and the phase angle increment (delta.  $\Delta$ ) between successive table accesses.

If delta is unity (i.e., the entries are read sequentially) and the table is accessed every T seconds (T is referred to as the sampling interval), the FTF of the sine wave synthesized will be:

$$FTF = 1/NT Hz$$
 Eqn. 2-1

On the other hand, if delta is greater than unity, e.g., every second ( $\Delta=2$ ) or third ( $\Delta=3$ ) entry is read, (see Figure 3-2) and the table is still accessed every T seconds, then the frequency of the sine wave synthesized will be:

$$f = \Delta \bullet FTF Hz; \ \Delta \le N/2$$
 Eqn. 2-2

If delta is an integer value, only multiples of the FTF can be generated; whereas, if delta is allowed to be fractional, any frequency up to the MSF can be generated. The maximum value delta can assume is N/2 since at least two samples per cycle are required to synthesize a sine wave without aliasing.

The value of the sample output, x(n), will depend on the initial phase angle, phi  $(\phi)$ , and the time or sample index, n, as follows:

$$x(n) = \sin[\phi + n \cdot \Delta \cdot 360/N]; \quad n = 0, 1, 2, ...$$
 Eqn. 2-3

The THD of the synthesized sine wave depends upon the length of the table, N, the accuracy (number of bits of precision) of the data stored in the table and the value of delta.

2-2 MOTOROLA

#### **SECTION 3**

## **Direct Table Look-Up**

# 3.1 Integer Delta Implementation

"When fractional values of delta are used, samples of points between table entries must be estimated using the table values."

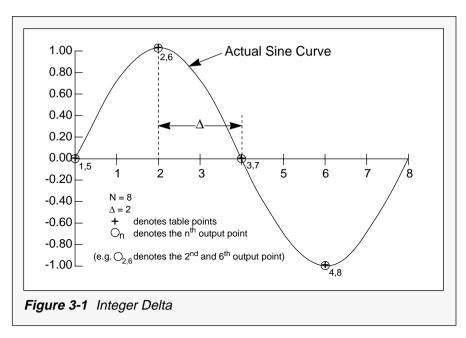
T his implementation is a direct table look-up method with delta being a positive integer number. Because delta is limited to being an integer all the required samples are contained within the table; no approximations are necessary. Figure 3-1 illustrates this method using N = 8 and  $\Delta$  = 2.

The assembler listing for the SINe-Wave Generation Integer Delta ("SINWGID") routine is presented in Figure 3-2. The corresponding memory map is shown in Figure 3-3.

Although no assembler options are indicated in this listing, a number of options are available. Refer to the Macro Assembler Reference Manual for information (6).

The memory locations can also be changed to suit the user's needs. In this routine the sine table (N=256) is in internal Y ROM starting at address HEX 100 to minimize external accesses and preserve RAM for data variables. The actual 256 sine table values stored are given in **Appendix B**. The output location is chosen to be an address in external I/O space, Y:\$FFE0.

The part of the routine that generates the sine samples is given in the form of a subroutine to facilitate calculation of the MSF. Only a MOVEP and a JMP instruction must be executed to output a sample point. This MOVEP instruction utilizes the modulo addressing capability of the DSP56001/2. Three address arithmetic unit registers are used in this routine; the address register, R1, contains the index into the sine table, the offset register, N1, contains the value of delta, and the modifier register, M1, contains the value N-1 to set up the modulo buffer.

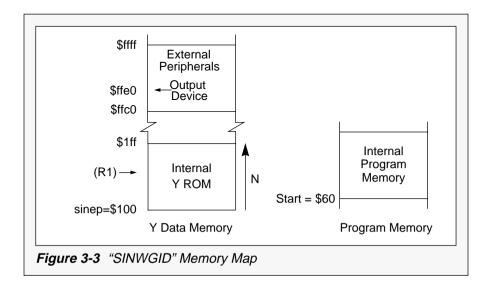


**NOTE:** In Figure 3-2, the numbers in the parentheses at the far right of the subroutine portion of the listing indicate the number of instruction cycles required to complete the specific instruction. These numbers have been manually included as comments to ease the calculation of MSF in Eqn. 3-1.

3-2 MOTOROLA

```
Motorola DSP56000 Macro Cross Assembler Version 1.10 06-18-87 13:03:01 sinwaid.asm
Page 1
               page 132.50.0.10
          ;SINWGID is a direct table look-up routine for SINE Wave Generation
3
          jusing Integer Delta values. The sine table is in on-chip ROM starting
4
          ;at address Y:$100 and contains 256 (N) entries which correspond to the
5
          sines of 256 equally spaced angles between 0 and 360 degrees.
6
          ;Integer delta values between 1 and N/2 can be used to step through the
7
          ;table. Here Delta=2 and is saved in N1. The table size is saved in M1.
8
9
    00000060
                                 $60
                                                      starting address.
                    ctart
                           ean
                           equ
10
   00000100
                    sinep
                                 $100
                                                      isine table starting address.
   000000FF
11
                    mask
                                 255
                                                      ;set mask = table size - 1.
                           eau
12
   00000002
                    delta
                                                      ;set delta = 2
                           eau
                                 2
13
    03770000
                    sinea
                           equ
                                 $ffe0
                                                      address of output device.
14
   P:0060
                           ora
                                 p:start
15
   P:0060
             0506BA
                                          #6, omr
                                                      ;enable on-chip ROM with sine table
                                 movec
                                                      ;initialize sine table pointer.
16
   P:0061
             61F400
                                          #sinep,r1
                           move
17
             000100
18 P:0063
             05FFA1
                                          #mask.ml
                                                      ; set up modulo N addressing.
                           movec
19
   P:0064
             390200
                           move
                                          #delta,n1
                                                      ; offset equals Delta.
20
   P:0065
             0BF080
                           isr
                                sinea
                                                      ; jump to subroutine.
21
             000066
22
   P:0067
             09C9E0 sineq
                           movep
                                          y:(r1)+n1,y:sinea
                                                             ;output sample.
23
   P:0068
             00000C
                                                             ;return from subroutine.(2)
                           rts
                                                             the end of listing.
                           end
0 Errors
0 Warnings
```

Figure 3-2 "SINWGID" Routine



Resources required for the "SINWGID" routine:

**Data ROM** 256 24-bit words for the sine table

Program Memory 6 24-bit words for the initialization 2 24-bit words for the subroutine

The MSF for the given sine-wave subroutine would be achieved by replacing the RTS instruction with the JMP SINEG instruction. After performing the above replacement, MSF is given by:

$$MSF = \frac{1}{2 \cdot lcyc \cdot SIC}$$
 Eqn. 3-1

where:

SIC = the total number of Subroutine
Instruction Cycles in "sineg".
SIC can be obtained by adding the
numbers in the brackets incorporated in the subroutine

Icyc = the instruction cycle execution time
For example, in Eqn. 3-1, if Icyc = 50 ns and SIC = 4 cycles:

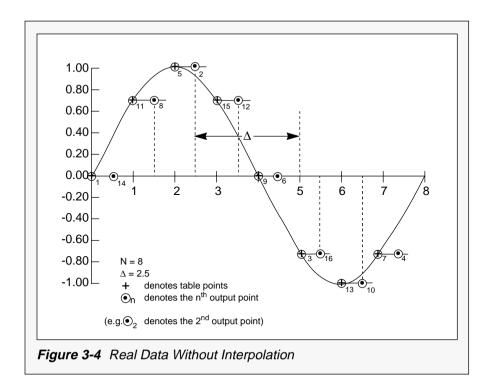
**MSF** = 
$$1/(2 \cdot 50 \cdot 4)$$
 MHz  
=  $2.5$  MHz

The results above compare very favorably in terms of both program memory requirements and execution speed with those for other competitive products (7).

3-4 MOTOROLA

#### 3.2 Real Delta Implementation

This implementation is a direct table look-up method with delta being a positive real number, that is, a number consisting of an integer and a fractional part. When fractional values of delta are used, samples of points between table entries must be estimated using the table values. The most straightforward estimation is to use the previous table entry. This approach is described in this section and illustrated in Figure 3-4 for N = 8 and  $\Delta$  = 2.5.

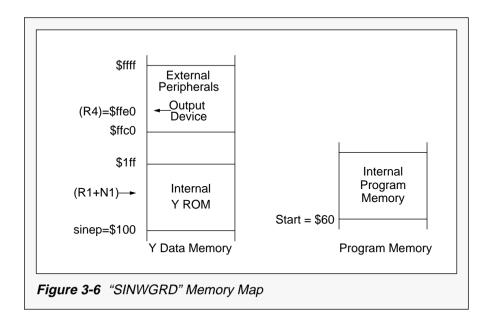


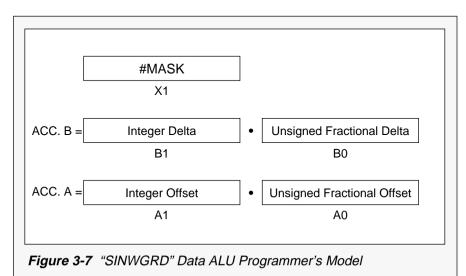
The assembler listing for the SINe-Wave Generation Real Delta ("SINWGRD") routine is presented in Figure 3-5. The memory map (see Figure 3-6) is the same as that used for the SINWGID routine except that R4 is used to point to the output device. This saves one cycle since the previous sample can be output while the accumulator is being updated using the parallel move feature of the DSP56001/2. The programmer's model for the Data ALU is presented in Figure 3-7.

```
Motorola DSP56000 Macro Cross Assembler Version 1.10 06-18-87 13:03:27 sinword.asm Page 1
                       132,50,0,10
          ;SINWGRD is a direct table look-up routine for SINe Wave Generation using
3
          positive Real numbers for Delta. The sine table is in on-chip ROM starting at
          address r:$100 and contains 256 (N) entries corresponding to the sine values
5
          of 256 equally spaced angles between 0 and 360 degrees. N must be a power of
6
          ; two. Delta can be between 0.0 and N/2. Here delta = 2.5 and is saved in B1 and
7
          ;BO. The table size minus one, N-1, is saved in X1.
R
9
    00000060
                    start equ $60
                                                          iprogram starting address.
10
   00000100
                    sinep equ $100
                                                          ; sine table starting address.
11
    000000FF
                   mask
                          eau $ff
                                                          iN - 1.
12 2.500000
                   delta equ 2.5
                                                         idelta = 2.5
13
    0333000
                   sinea equ $ffe0
                                                         ;address of output device.
14
   P:0060
                          org p:start
15 P:0060 0506BA
                              movec #6,omr
                                                         ;enable on-chip ROM with sine table
16
   P:0061 64F400
                                      #sinea.r4
                                                         ;set up output pointer.
                          move
16
             033300
   P:0063
17
             51F400
                                      #(delta-@cvi(delta)),b0;store fract. part in b0.
                          move
18
             400000
19
   P:0065
             61F43A
                          asl b
                                      #sinep, r1
                                                         ;eliminate sign bit, init. rl.
20
             000100
21 P:0067
             2D0200
                          move
                                      #acvi(delta),bl
                                                        ;integer part of delta in bl.
22
    P:0068
             390013
                                                         ;initialize acc. a and n1.
                          clr a
                                      #0.n1
23 P:0069
             45F400
                          move
                                      #>mask, x1
                                                         ;set modulo mask.
24
             0000FF
   P:006A
25
                                                         ; jump to subroutine.
             0BF080
                          jsr sineg
26
             00006C
27 P:006C
             4EE910 sineg add b,a
                                              y:(r1+n1),y0;update a, get sine value.
                                                                                       (2)
28 P:006D
             4E6466
                          and x1, a
                                              y0,y:(r4) ;mask a, output sample.
                                                                                       (1)
29
    P:006E
             219900
                                     a1.n1
                                                         ;update offset register nl.
                          move
                                                                                       (1)
30
   P:006F
             00000C
                          rts
                                                         return from subroutine.
                                                                                       (2)
31
                          end
                                                         ;end of listing.
0 Errors
0 Warnings
```

Figure 3-5 "SINWGRD" Routine

3-6 MOTOROLA





Given delta is now a real number, the inherent modulo addressing mode in the DSP56001/2. cannot be used and therefore a modulo addressing scheme must be implemented in software. The following is a description of one approach to implementing such a scheme. This approach uses both accumulators.

In this routine the integer part of delta is stored in the upper portion of an accumulator (B1 for the example given), and the fractional part is stored in the lower portion of the same accumulator (B0). Care should be taken to ensure that the fractional part is stored correctly. The number moved into B0 as a result of subtracting the integer portion from delta, i.e.  $\Delta$  -@cvi( $\Delta$ ), is a signed, i.e. positive, fraction. This is undesirable since the sign bit should be associated with the integer portion. Therefore a shift to the left must be performed to eliminate the sign bit leaving the unsigned fraction in B0.

The separation of integer and fractional portions is done by using the assembler "ConVert to Integer" built-in function (@cvi). The CVI function converts real numbers to integers by simply truncating the fractional part of the number. Therefore:

- @cvi(Δ) returns the integer portion of delta
- Δ-@cvi(Δ) returns the signed fractional part of delta

This assumes that delta is not a runtime variable. If delta is required to be a runtime variable, it can be passed by separating it into a signed integer and unsigned fraction which are loaded into B1 and B0 respectively.

3-8 MOTOROLA

A second accumulator, A in this example, contains the positive real number value used to load the offset register, N1, which is used to offset the pointer, R1. R1 is used to address the correct location in the sine table. Since the table index must be an integer, only A1 is moved to N1. Incrementing by delta, however, is done on both the integer and fractional parts of the A accumulator. It should be noted that the increment of the register R1 is done by indexing the register with the offset register N1, thus leaving the original value of R1 (base address) unchanged. Note that the binary point is at an imaginary point between the two 24-bit parts of the accumulators. Initially we have:

After the first addition we get:

To wrap the pointer, A1, around when it is incremented past the length of the table, a masking operation is performed on A. The mask, contained in X1, is the table length minus one, N-1, where N is restricted to be a power of two. This restriction is necessary to ensure that the mask consists of k least significant ones where k is defined by 2k = N. Using the above masking operation, the value of A1 and consequently N1, is restricted to be between 0 and N-1.

Resources required for the "SINWGRD" routine:

**Data ROM** 256 24-bit words for the sine table

**Program Memory** 11 24-bit words for the initialization

4 24-bit words for the subroutine memory

**MSF** 1/(2 • 50 • 6) MHz

= 1.667 MHz

#### 3.3 Harmonic Distortion

Due to the fact that the sine wave generated is an approximation, not all of the energy is at the fundamental frequency; a certain amount of the energy of the generated samples falls into frequencies other than the fundamental. Those frequencies are:

- 1. Harmonic frequencies, hf, i.e. integer multiplies of the fundamental frequency, f
- Subharmonic frequencies, sf, where s = h/d and h, d are integers

The resulting noise is measured in terms of THD, given by the following equation:

THD =  $\frac{\text{spurious harmonic energy}}{\text{total energy of the waveform}}$  Eqn. 3-2

When using the table look-up algorithms, harmonic

3-10 MOTOROLA

#### distortion occurs from two distinct sources —

 Quantization Error: Since the sine table values stored in memory are of finite word length (24 bits in this case) the sine values cannot be represented exactly. Quantization error is directly proportional to the word length. For example the sine of 45 degrees in decimal will be:

0.7070707 using 24 bits

0.7071 using 16 bits

 Sampling Error: When points between table entries are sampled, i.e., delta is not an integer, then large errors are introduced because these points must be estimated from the table values. Since the sampling errors are derived from the table values, sampling errors are always greater than quantization errors.

The THD for different deltas and different table sizes is shown in Table 3-1(a), Table 3-1(b), and Table 3-2.

Table 3-1(a) Total Harmonic Distortion — Integer Delta

N	$\Delta = 2$	$\Delta = 3$
8	3.5527141 • 10 <sup>-15</sup>	5.7949068 • 10 <sup>-15</sup>
16	5.7949068 • 10 <sup>-15</sup>	3.6274700 • 10 <sup>-15</sup>
32	3.6274700 • 10 <sup>-15</sup>	2.8356370 • 10 <sup>-15</sup>
64	2.8356370 • 10 <sup>-15</sup>	3.4157912 • 10 <sup>-15</sup>
128	3.4157912 • 10 <sup>-15</sup>	2.8659804 • 10 <sup>-15</sup>
256	2.8659804 • 10 <sup>-15</sup>	2.6423040 • 10 <sup>-15</sup>
512	2.6423040 • 10 <sup>-15</sup>	2.6142553 • 10 <sup>-15</sup>
1024	2.6142553 • 10 <sup>-15</sup>	2.4857831 • 10 <sup>-15</sup>

3-12 MOTOROLA

Table 3-1	(b) Total Harmonic Dist	ortion — Integer Delta
Δ	N = 64	N = 256
1	3.4157912 • 10 <sup>-15</sup>	2.6423040 • 10 <sup>-15</sup>
2	2.8356370 • 10 <sup>-15</sup>	2.8659804 • 10 <sup>-15</sup>
3	3.4157912 • 10 <sup>-15</sup>	2.6423040 • 10 <sup>-15</sup>
4	3.6274702 • 10 <sup>-15</sup>	3.4157912 • 10 <sup>-15</sup>
5	3.4157912 • 10 <sup>-15</sup>	2.6423040 • 10 <sup>-15</sup>
6	2.8356370 • 10 <sup>-15</sup>	2.8659804 • 10 <sup>-15</sup>
7	3.4157912 • 10 <sup>-15</sup>	2.6423040 • 10 <sup>-15</sup>
8	5.7949069 • 10 <sup>-15</sup>	2.8356370 • 10 <sup>-15</sup>
9	3.4157912 • 10 <sup>-15</sup>	2.6423040 • 10 <sup>-15</sup>
10	2.8356370 • 10 <sup>-15</sup>	2.8659804 • 10 <sup>-15</sup>

Ta	Table 3-2         Total Harmonic Distortion — Real Delta												
	N = 64	N = 128	N = 256										
	2.8356370 • 10 <sup>-15</sup>	3.4157912 • 10 <sup>-15</sup>	2.8659804 • 10 <sup>-15</sup>										
	7.5141324 • 10 <sup>-04</sup>	1.8539830 • 10 <sup>-04</sup>	4.7061084 • 10 <sup>-05</sup>										
	6.0107522 • 10 <sup>-04</sup>	1.4805426 • 10 <sup>-04</sup>	3.7649080 • 10 <sup>-05</sup>										
	7.5141324 • 10 <sup>-04</sup>	1.8539830 • 10 <sup>-04</sup>	4.7061084 • 10 <sup>-05</sup>										
	3.4157912 • 10 <sup>-15</sup>	2.8659804 • 10 <sup>-15</sup>	2.6423040 • 10 <sup>-15</sup>										
	7.5141324 • 10 <sup>-04</sup>	1.8539830 • 10 <sup>-04</sup>	4.7061084 • 10 <sup>-05</sup>										
5	7.9041085 • 10 <sup>-04</sup>	1.9724369 • 10 <sup>-04</sup>	4.9414069 • 10 <sup>-05</sup>										

The equations as well as the FORTRAN code used for calculating the THD in the above tables are included in **Appendix A**. With respect to Table 3-1(a), Table 3-1(b), and Table 3-2 some important observations and conclusions can be drawn:

- 1. For integer delta the THD for  $N \le 1024$  is of the same order of magnitude. This can be seen in Table 3-1(a) and Table 3-1(b). For integer deltas the only errors which cause distortion are quantization errors.
- 2. For integer delta and small N the THD is nonuniform. This is evident for  $\Delta = 2$  and N  $\leq$  128 or  $\Delta = 3$  and N  $\leq$  64 in Table 3-1(a). For small N, the quantization error distribution is not uniformly distributed between  $\pm 1/2$  Least Significant Bit (LSB) thereby causing the THD values to be nonmonotonic.
- 3. For integer delta and large N the THD decreases monotonically with increasing N. This is evident for  $\Delta=2$  and N  $\leq$  128 or  $\Delta=3$  and N  $\leq$  64 in Table 3-1(a). For large N, the quantization error distribution will tend to be uniform between  $\pm$  1/2 LSB resulting in the monotonic behavior.
- 4. THD for odd deltas and any N is constant. Similarly, THD for even deltas and any N is constant with the exception of delta equal to a power of two greater than 2 (see Table 3-1(b)). The explanation rests with the observation that all N points are used for generating sine waves using odd deltas. The N/2 even points are used twice for generating sine waves using even deltas with the exception of delta being a power of two greater than 2. For this exception, the points used in generating the sine waves are separated by delta and are used delta times. As noted in Appendix A, for integer deltas the total number of points used in the THD calculations will be independent of delta and equal to N.

3-14 MOTOROLA

- 5. THD depends on the fractional part of delta. The THD for  $\Delta$  = 2.50 is less than either 2.25 or 2.75 (see Table 3-2), because the fractional part generates an integer every other access for  $\Delta$  = 2.50 and every other fourth access for 2.25 or 2.75. Therefore, every other sample is free of sampling error for  $\Delta$  = 2.5 but only every fourth sample is free of sampling error for the other two cases. Observe that the THD for 2.25, 2.75, and 8.25 is the same. The THD for 11.625 is slightly higher because the fractional part forms an integer only every eighth access.
- 6. The THD for non-integer deltas decreases with increasing table length as seen in Table 3-2. Consider the same delta entries for different N. By increasing the table length, the difference between table entries decreases, resulting in better approximations to the non-integer samples, hence reduced sampling errors.

3-15 MOTOROLA

#### **SECTION 4**

# Table Look-Up with Linear Interpolation

". . . the THD improves dramatically for non-integer values of delta when using interpolation."

In order to synthesize a sine wave of any frequency with low distortion, an interpolation method must be used together with table look-up. By using interpolation, sine values between table entries can be represented more accurately. The easiest interpolation technique to implement is linear interpolation. For linear interpolation the sine value for a point between successive table entries is assumed to lie on the straight line between the two values. This is illustrated in Figure 4-1 where  $\Delta = 2.5$  and N = 8. Contrast this figure with Figure 3-4.

The algorithm used for linear interpolation is based on the equation of a straight line:

$$y = m \cdot x + b$$

where: m = the slope of the line

x = the x-coordinate value

b = the initial y value

y = the new y value

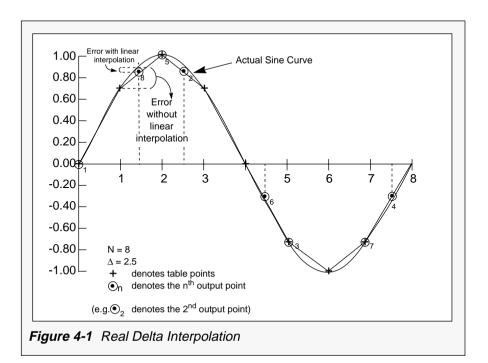
#### For linear interpolation:

- m = S[i + 1] S[i]; i.e., it is the slope of the line segment between successive table entries i and i + 1
- b = S[i], the value of the sine table at the base address plus the i<sup>th</sup> offset location
- x =the fractional part of the pointer,

y = S[i + x], the approximated sample value

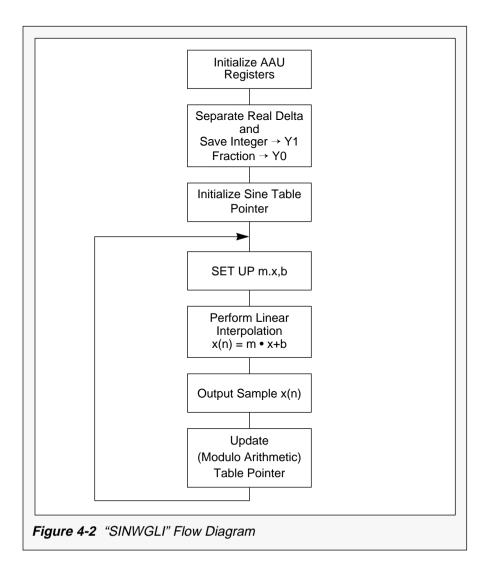
Therefore, we have:

$$S[i+x] = S[i]+x \bullet \{S[i+1]-S[i]\}$$



4-2 MOTOROLA

The program flow diagram for the SINe-Wave Generation Linear Interpolation ("SINWGLI") routine is presented in Figure 4-2.



The assembler listing is given in Figure 4-3; the memory map is presented in Figure 4-4; and the Data ALU programmer's model is presented in Figure 4-5.

The sine table is stored in Y ROM starting at HEX 100. The address pointer, R1, points to the current sine value while address pointer, R2, points to the current plus one sine value, R2=R1+1. The slope between successive points is determined by subtracting the table entry pointed to by R2 from the table entry pointed to by R1.

For the "SINWGLI" routine, the fractional part of the linear approximation, x, is stored in the accumulator, A0, and the integer portion is stored in A1. A1 is "moved" into N1 which is used to index the R1 register. The same value that is moved in N1 is moved in N2 which is used to index R2. Note that in contrast to the "SINWGRD" routine, the content of A0 has to be right shifted so that it is in the correct positive signed fractional format prior to performing the multiplication to generate the linear approximation. Delta can be any positive real number between 0.0 and N/2. Accumulator B is first used to separate delta into a signed integer and an unsigned fraction (see "SINWGRD" routine), and then it is used to calculate the interpolated sample value. Note that an immediate long move (i.e., using the ">" sign) must be specified when saving the integer part of delta in Y1 because ( $@CVI(\Delta)$ ) would be interpreted as a signed fraction otherwise (8). The part of the routine that generates the sine samples is given in the form of a subroutine.

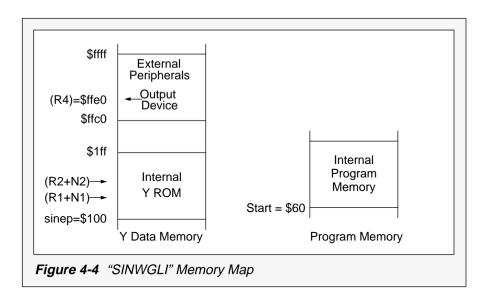
4-4 MOTOROLA

		y0.																							(1)	(2)	(5)	(1)	(5)	(1)	(T)	Œ.	Œ.	Ð,	(1)	E 9	(7)
9 sinwgli.asm Page 1	page 132,50,0,10 SINWGLI is a direct table look-up routine for SINe Wave. Generation using Linear Interpolation	with any positive real delta greater than 0.0 and less than N/2.0. Here delta = 2.5 and is saved in y1 and y0.	256 equally spacedangles	inus one, N-1, is saved in NO.	program starting address	sine table starting address:	;base address plus N minus one	delta = 2.5	;address of output device		enable on-chip ROM with sine table	set up output pointer;	store fraction part in b0	•	eliminate sign bit, initialize rl	integer part of Delta in yl		unsigned fractional Delta in y0	initialize a and nl;	set up mask value	initialize n2	initialize r2 with the value r1+1	editionalis of amilia		fraction part of ptr in bl, b0=0	;bl=signed fr. Delta, x0=sine	sign. fract. in x1, sine in bl	subtr sines to obtain slope:	slope value to x0, sine in bl	sample approximation = m*x+b	'update calculation, output sample	set up mask value in xl	mask al = modulo arithmetic	update offset register nl	update offset register n2	return from the subroutine	the end of the routine
Motorola DSP56000 Macro Cross Assembler Version 1.10 06-18-87 17:19:09 sinwgli.asm Page 1	outine for SINe Waye. Generat	ian $0.0$ and less than $N/2.0$ . Here	The sine table contains 256 (N) entries corresponding to the sines of 256 equally spacedangles	; between 0 and 360 degrees. N must be a power of two. The table size minus one, N-1, is saved in NO							#6, omr	#sinea, r4	#(delta @cvi(delta)),bo		#sinep, rl	#>@cvi(delta),yl		b0,y0	#0, n1	#mask, n0	#0, n2	#sinep+1,r2			a0,b		bl,xl y: (r2+n2),b		b,x0 y:(r1+n1),b		b,y:(r4)	no,xl	ī	al,nl	al,n2		
mbler V	k-up ro	ater th	entries	st be a	\$60	\$100	\$££	2.5	\$ffe0	p:start	movec				Д				В				500	5		Q		a, ox		x0,x1,b	У, а		xI,a				
oss Asser	132,50,0,10 ect table loc	delta gre	s 256 (N)	ees. N mus	edn	eđn	edn	edn	edn	org		move	move		asl	move		move	clr	move	move	move	Ş.	i.	move	lsr	move	qns	move	macr	add	move	and	move	move	rts	end
Macro Cr	direct	tive real	e contain	360 degr	start	sinep	mask	delta	sinea																sineg												
P56000	page LI is a	isod yu	ne tabl	in 0 and	_	_		_	_		0506BA	64F4UU	51F400	400000	61F43A	47F400	000002	212600	390013	38FF00	3A0000	62F400	0000101	000000	210F00	4CE92B	1FEA00	20004C	1BE900	2000AB	5F6430	230500	200066	219900	219A00	000000	
rola DE	; SINWG	; with a	; The si	; betwee	09000000	000000100	000000EF	2.500000	0000FFE0	P:0060	P:0060	T900:d	P:0063		P:0065	P:0067		P:0069	P:0070	P:006A	P:006B	P:006C	D.006		P:0070	P:0071	P:0072	P:0073	P:0074	P:0075	P:0076	P:00.77	P:0078	P:00.79	P:007A	P:00.7B	34 0 Errors
Moto	Н	7	м	4	D.	9	7	œ	0	10	11	7.7	13		14	15		16	17	18	19	20	21	1	22	23	24	25	26	27	28	52	30	31	32	 	34 0 Er

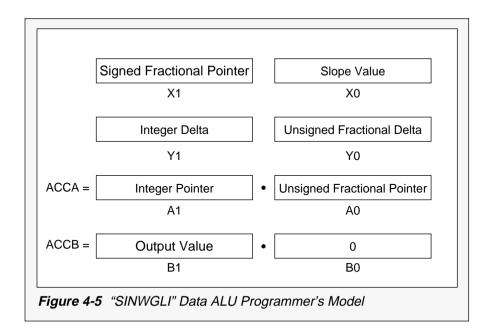
### MOTOROLA 4-5

Figure 4-3 "SINWGLI" Routine

Six address arithmetic unit registers are used in this routine; besides R1, R2, R4, N1, and N2, the modifier register M2 is used. The use of M2 is twofold. First, M2 is used to store the mask value before it is used in the AND masking operation. (This masking operation constrains R1 + N1 within the desired region in memory, i.e., implements modulo addressing.) Second, it is used to activate modulo arithmetic updates of R2 + N2. This is necessary to take care of the special case where R1 +N1 points to \$1FF. Since R2 + N2 equals R1 + N1 + 1, it would point to \$200 instead of \$100 without modulo arithmetic.



4-6 MOTOROLA



Resources required for the "SINWGLI" routine:

**Data ROM** 256 24-bit words for the sine table

**Program Memory** 17 24-bit words for the initialization

12 24-bit words for the program memory

**MSF**  $1/(2 \cdot 50 \cdot 16) \text{ MHz} = 0.625 \text{ MHz}$ 

#### 4.1 Harmonic Distortion

As expected the THD improves dramatically for non-integer values of delta when using linear interpolation. This is of course because the intermediate points are better approximated. The performance for integer deltas remains the same as that for the direct table look-up methods already discussed. The results for the THD using linear interpolation are shown in Table 4-1 and these results should be directly compared with the results in Table 3-2.

Table 4-1 Total Harmonic Distortion — Real Delta						
Δ	N = 64	N = 128	N = 256			
2.00	2.8356370 • 10 <sup>-15</sup>	3.4157912 • 10 <sup>-15</sup>	2.8659804 • 10 <sup>-15</sup>			
2.25	2.0443282 • 10 <sup>-07</sup>	1.2762312 • 10 <sup>-08</sup>	7.9741605 • 10 <sup>-10</sup>			
2.50	3.6316863 • 10 <sup>-07</sup>	2.2683957 • 10 <sup>-08</sup>	1.4175620 • 10 <sup>-09</sup>			
2.75	2.0443282 • 10 <sup>-07</sup>	1.2762312 • 10 <sup>-08</sup>	7 9741605 • 10 <sup>-10</sup>			
3.00	3.4157912 • 10 <sup>-15</sup>	2.8659804 • 10 <sup>-15</sup>	2.6423040 • 10 <sup>-15</sup>			
8.25	2.0443282 • 10 <sup>-07</sup>	1.2762312 • 10 <sup>-08</sup>	7.9741605 • 10 <sup>-10</sup>			
11.625	1.4913862 • 10 <sup>-07</sup>	9.3069933 • 10 <sup>-09</sup>	5.8146748 • 10 <sup>-10</sup>			

4-8 MOTOROLA

With respect to Table 4-1 some important observations and conclusions can be drawn:

- THD is reduced by 103 by using linear interpolation with direct table look-up. This can be verified by comparing Table 3-2 with Table 4-1. This is because an extra correctional value is added to the sine value obtained from the sine table. This correctional value is the product of the slope at the specific point and the fractional part of the pointer (i.e., m-x).
- THD depends only on the fractional part of delta when linear interpolation is used. It is a maximum for the fractional part = 0.5 and symmetrical about this midpoint. This is evident in Table 4-1. This is because the linear approximation is poorest at the midpoint.

#### **APPENDIX A**

# Computation of Total Harmonic Distortion (THD)

"To determine the precision needed to calculate THD, consider the inherent symmetry in the DFT." The equation for calculating THD (given in Eqn. 3-2) can be rewritten as:

$$THD = \frac{ET - EF}{ET}$$
 Eqn. A-1

where: ET = the total energy of the wave
EF = the energy of the fundamental
frequency

For accurate and correct results, the above energy terms must be calculated over a full cycle of the synthesized sine wave. In the case of direct table lookup, a full cycle may require several passes through the sine table. The number of passes depends on the value of delta used.

A full cycle will be synthesized for the smallest n for which n •  $\Delta$  is evenly divisible by N. For example, if the table length, N = 128, and the step size,  $\Delta$  = 2.5 = 5/2, then a complete cycle occurs for n = 256, since 256 • 2.5/128 = 5. Figure 3-4 illustrates an example for N = 8 and  $\Delta$  = 2.5. The (2 • 8 =) 16 points required for the THD calculation are shown on the figure.

In general, if  $\Delta = A/B$ , where A and B are relatively prime numbers, then the minimum number of samples, N', which must be output to synthesize a full cycle is N' = B • N.

The total energy, ET, in a cycle of length BN (BN =  $B \cdot N$ ) is given by:

$$\mathsf{ET} = \sum_{i \, = \, 0}^{\mathsf{BN} \, - \, 1} x(i) \cdot x(i) \qquad \qquad \mathsf{Eqn.} \; \mathsf{A-2}$$

where: x(i) is the i<sup>th</sup> sample of the sine-wave sequence

The amount of energy in the fundamental frequency, EF, over the same period is given by:

EF = 
$$(1/BN) \cdot (|X(A)|^2 + |X(BN - A)|^2)$$
  
=  $(2/BN) \cdot (|X(A)|^2)$  for a real sequence

Eqn. A-3

where the X(k) are terms of the Discrete Fourier Transform (DFT) defined by the following equation:

$$X(k) = \sum_{n=0}^{BN-1} x(n)e^{[-j(2 \cdot \pi/BN) \cdot n \cdot k]}$$
 Eqn. A-4

The x(n) values used to calculate THD in Table 3-1(a), Table 3-1(b), Table 3-2, and Table 4-1 are based on actual values computed by the DSP56001/2 for the 3 sample sine-wave generator programs described in this document. The THD computation was carried out using VAX VMS FORTRAN and by using the formulas given above with double precision floating point arithmetic(9).

A-2 MOTOROLA

The VAX VMS FORTRAN source code used for the computation of THD is given in Figure A-1.

Some important details concerning the computation of the THD should be noted. ENERG3 and (ENERG2-EFUND) ideally should have the same value. However, a difference may occur because ENERG2 is much greater than EFUND. The result of the subtraction will be inaccurate due to numerical precision limitations. To determine the precision needed to calculate THD, consider the inherent symmetry in the DFT. For a real sequence x(n), the DFT sequence, X(k), exhibits the following symmetries (10):

- 1.  $Re\{X(k)\} = Re\{X(N-k)\}$
- 2.  $Im\{X(k)\} = -Im\{X(N k)\}$
- 3.  $Mag{X(k)} = Mag{X(N k)}$
- 4.  $Arg\{X(k)\} = Arg\{X(N k)\}$

where: N is the length of the DFT

Therefore, using symmetry 3 as a check for the correct results for N = 128, we should have:

$$\label{eq:mag} \begin{split} \text{Mag}\{X(1)\} &= \text{Mag}\{X(127)\} \\ \text{Mag}\{X(2)\} &= \text{Mag}\{X(126)\} \\ & \bullet \\ & \bullet \\ \\ \text{Mag}\{X(n)\} &= \text{Mag}\{X(128 - n)\} \end{split}$$

MOTOROLA A-3

This, in turn, means that the following equalities should hold:

$$\begin{aligned} \cos(2 \bullet \pi \bullet k \bullet n/N) &= \cos(2 \bullet \pi \bullet (N-k) \bullet n/N) \\ \sin(2 \bullet \pi \bullet k \bullet n/N) &= -\sin(2 \bullet \pi \bullet (N-k) \bullet n/N) \\ &= \operatorname{Eqn. A-5} \end{aligned}$$

where: 
$$n = 0,1,2,...BN-1$$
  
 $k = 0.1.2...BN-1$ 

If single precision accuracy is used in calculating the THD, the above equalities do **NOT** hold. For example,

let 
$$k = 1$$
  
 $n = 128$   
 $ARG1 = 2 \cdot \pi \cdot n \cdot 1/128$   
 $ARG2 = 2 \cdot \pi \cdot n \cdot 127/128$ 

Then, as shown in Table A-1, cos (ARG1) does not equal cos (ARG2) when truncating to only 8 digits. If, however, double precision is used, the equalities of Eqn. A-5 are satisifed, as shown in Table A-2 even when truncating to 10 digits.

Table A-1 Single Precision Accuracy				
n	cos(ARG1)	cos(ARG2)	sin(ARG1)	-sin(ARG2)
125	0.9891766	0.9891724	0.1467302	-0.1467580
126	0.9951848	0.9951788	0.0980167	-0.0980776
127	0.9987954	0.9987938	0.0490676	-0.0491002

Table A-2 Double Precision Accuracy				
n	cos(ARG1)	cos(ARG2)	sin(ARG1)	-sin(ARG2)
125	0.989176509	0.989176509	0.146730474	-0.146730474
126	0.995147266	0.995147266	0.098017140	-0.098017140
127	0.998795456	0.998795456	0.049067674	-0.049067674

A-4 MOTOROLA

```
Program THD FOR Using double precision real arithmetic
  Program to calculate THD for digital sine-wave generation without interpolation.
    TMPLTCTT COMPLEX*16(X)
    REAL*8 ENERG1 ENERG2 ENERG3 S(2048) TWOPT TSS(2048)
    DIMENSION X(0:2048)
    INTEGER*4 IS(2048)
    TYPE *.' ENTER TABLE SIZE (UP TO 2048)'
    ACCEPT *,NN
    TYPE *.'ENTER INPUT HEX FILENAME'
    the hex values are assumed to be 11 on each line, each consisting of 6 characters of
and having a blank space in between them. This is the format of the "LOD" file
   that is generated by the assembler [5].
    READ(1.110)(TS(T).T=1.NN)
110 FORMAT(11(76.X))
   DO 120 I=1.NN
    IF(BTTEST(IS(I),23)) THEN
         IS(I)=JIOR(IS(I),'FF000000'X)
    ENDIF
120 CONTINUE
    DO 100 I=2,NN
    ISS(I)=IS(I)
100 CONTINUE
   TYPE *,' ENTER DELTA, BN, A' ACCEPT *, DELTA, BN, A
    AINDEX=0.0
    DO 200 TABC=1.BN
    TNDEX=TNT(ATNDEX)
    S(IABC)=DBLE(ISS(INDEX+1))
    ATNDEX=ATNDEX+DELTA
    IF (AINDEX.GT.FLOAT(N)) AINDEX=AINDEX-FLOAT(N)
200 CONTINUE
    TWOPI=8.0*DATAN(1.D0)
    DO 400 TK=0.BN-1
    XSUM=DCMPLX(0.D0,OD0)
    DO 300 IN=0,BN-1
    XARG=DCMPLX(0.D0,-TWOPI*DBLE(IN)*DBLE(IK)/DBLE(BN))
300 XSUM=XSUM+DCMPLX(S(IN+1),0.D0)*CDEXP(XARG))
    X(TK)=XSUM
400 CONTINUE
    DO 500 IK=0.BN-1
500 ENERG1=ENERG1+CDABS(X(IK))**2.D0)
    ENERG1=ENERG1/DBLE(BN)
    DO 505 IR=0.BN-1
    IF((IK.EQ.(A)).OR.(IK.EQ.(BN-INT(A)))) GOTO 505
    ENERG3=ENERG3+(CDABS(X(IK))**2.D0)
505 CONTINUE
    ENERG3=ENERG3/DBLE(BN)
    energ3 should be the same as EFUND
   DO 600 I=1.BN
600 ENERG2=ENERG2+(S(I)*S(I))
    TYPE *,' ENERG1=',ENERG1,' ENERG2=',ENERG2,'
    $ENERG3=',ENERG3
    EFUND=((CDABS(X(A))**2)+(CDABS(X(BN-A))**2))/DBLE(BN)
    TYPE * .' THD=' .ENERG3/ENERG2 .'EFUND=' .EFUND
    END
```

Figure A-1 VAX VMS FORTRAN Source Code for THD Computation

MOTOROLA A-5

## **APPENDIX B**

## The Sine Table

Table B-1 gives the sine entries for N=256. The hexadecimal values are given in the signed fractional format used for the DSP56001. "\$" denotes a hexadecimal value.

Table B-1 Sine Table

ADDRESS	VALUE
S_01	\$03242B
S_02	\$0647D9
S_03	\$096A90
S_04	\$0C8BD3
S_05	\$0FAB27
S_06	\$12C810
S_07	\$15E214
S_08	\$18F8B8
S_09	\$1C0B82
S_0A	\$1F19F9
S_0B	\$2223A5
S_0C	\$25280C
S_0D	\$2826B9
S_0E	\$2B1F35
S_0F	\$2E110A
S_10	\$30FBC5
S_11	\$33DEF3

ADDRESS	VALUE
S_12	\$36BA20
S_13	\$398CDD
S_14	\$3C56BA
S_15	\$3F174A
S_16	\$41CE1E
S_17	\$447ACD
S_18	\$471CED
S_19	\$49B415
S 1A	\$4C3FE0
S_1B	\$4EBFE9
S_1C	\$5133CD
S_1D	\$539B2B
S_1E	\$55F5A5
S_1F	\$5842DD
S_20	\$5A827A
S_21	\$5CB421
S_22	\$5ED77D

MOTOROLA B-1

 Table B-1
 Sine Table (continued)

ADDRESS	VALUE
S_23	\$60EC38
S_24	\$62F202
S_25	\$64E889
S_26	\$66CF81
S_27	\$68A69F
S_28	\$6A6D99
S_29	\$6C2429
S_2A	\$6DCA0D
S_2B	\$6F5F03
S_2C	\$70E2CC
S_2D	\$72552D
S_2E	\$73B5EC
S_2F	\$7504D3
S_30	\$7641AF
S_31	\$776C4F
S_32	\$788484
S_33	\$798A24
S_34	\$7A7D05
S_35	\$7B5D04
S_36	\$7C29FC
S_37	\$7CE3CF
S_38	\$7D8A5F
S_39	\$7E1D94
S_3A	\$7E9D56
S_3B	\$7F0992

ADDRESS	VALUE
S_3C	\$7F6237
S_3D	\$7FA737
S_3E	\$7FD888
S_3F	\$7FF622
S_40	\$7FFFF
S_41	\$7FF622
S_42	\$7FD888
S_43	\$7FA737
S_44	\$7F6237
S_45	\$7F0992
S_46	\$7E9D56
S_47	\$7E1D94
S_48	\$7D8A5F
S_49	\$7CE3CF
S_4A	\$7C29FC
S_4B	\$7B5D04
S_4C	\$7A7D05
S_4D	\$798A24
S_4E	\$788484
S_4F	\$776C4F
S_50	\$7641AF
S_51	\$7504D3
S_52	\$73B5EC
S_53	\$72552D
S_54	\$70E2CC

B-2 MOTOROLA

 Table B-1
 Sine Table (continued)

ADDRESS	VALUE
S_55	\$6F5F03
S_56	\$6DCA0D
S_57	\$6C2429
S_58	\$6A6D99
S_59	\$68A69F
S_5A	\$66CF81
S_5B	\$64E889
S_5C	\$62F202
S_5D	\$60EC38
S_5E	\$5ED77D
S_5F	\$5CB421
S_60	\$5A827A
S_61	\$5842DD
S_62	\$55F5A5
S_63	\$539B2B
S_64	\$5133CD
S_65	\$4EBFE9
S_66	\$4C3FE0
S_67	\$49B415
S_68	\$471CED
S_69	\$447ACD
S_6A	\$41CE1E
S_6B	\$3F174A
S_6C	\$3C56BA
S_6D	\$398CDD

ADDRESS	VALUE
S_6E	\$36BA20
S_6F	\$33DEF3
S_70	\$30FBC5
S_71	\$2E110A
S_72	\$2B1F35
S_73	\$2826B9
S_74	\$25280C
S_75	\$2223A5
S_76	\$1F19F9
S_77	\$1C0B82
S_78	\$18F8B8
S_79	\$15E214
S_7A	\$12C810
S_7B	\$0FABD
S_7C	\$0C8BD3
S_7D	\$096A90
S_7E	\$0647D9
S_7F	\$03242B
S_80	\$00000
S_81	\$FCDBD5
S_82	\$F9B827
S_83	\$F69570
S_84	\$F3742D
S_85	\$F054D9
S_86	\$ED37F0

MOTOROLA B-3

 Table B-1
 Sine Table (continued)

ADDRESS	VALUE
S_87	\$EA1DEC
S_88	\$E70748
S_89	\$E3F47E
S_8A	\$E0E607
S_8B	\$DDDC5B
S_8C	\$DAD7F4
S_8D	\$D7D947
S_8E	\$D4E0CB
S_8F	\$D1EEF6
S_90	\$CF043B
S_91	\$CC210D
S_92	\$C945E0
S_93	\$C67323
S_94	\$C3A946
S_95	\$C0E8B6
S_96	\$BE31E2
S_97	\$BB8533
S_98	\$B8E313
S_99	\$B64BEB
S_9A	\$B3C020
S_9B	\$B14017
S_9C	\$AECC33
S_9D	\$AC64D5
S_9E	\$AA0A5B
S_9F	\$A7BD23

ADDRESS	VALUE
S_A0	\$A57D86
S_A1	\$A34BDF
S_A2	\$A12883
S_A3	\$9F13C8
S_A4	\$9D0DFE
S_A5	\$9B1777
S_A6	\$99307F
S_A7	\$975961
S_A8	\$959267
S_A9	\$93DBD7
S_AA	\$9235F3
S_AB	\$90A0FD
S_AC	\$8F1D34
S_AD	\$8DAAD3
S_AE	\$8C4A14
S_AF	\$8AFB2D
S_B0	\$89BE51
S_B1	\$8893B1
S_B2	\$877B7C
S_B3	\$8675DC
S_B4	\$8582FB
S_B5	\$84A2FC
S_B6	\$83D604
S_B7	\$831C31
S_B8	\$8275A1

B-4 MOTOROLA

Table B-1 Sine Table (continued)

ADDRESS	VALUE
S_B9	\$81E26C
S_BA	\$8162AA
S_BB	\$80F66E
S_BC	\$809DC9
S_BD	\$8058C9
S_BE	\$802778
S_BF	\$8009DE
S_C0	\$800000
S_C1	\$8009DE
S_C2	\$802778
S_C3	\$8058C9
S_C4	\$809DC9
S_C5	\$80F66E
S_C6	\$8162AA
S_C7	\$81E26C
S_C8	\$8275A1
S_C9	\$831C31
S_CA	\$83D604
S_CB	\$84A2FC
S_CC	\$8582FB
S_CD	\$8675DC
S_CE	\$877B7C
S_CF	\$8893B1
S_D0	\$89BE51
S_D1	\$8AFB2D

ADDRESS	VALUE
S_D2	\$8C4A14
S_D3	\$8DAAD3
S_D4	\$8F1D34
S_D5	\$90A0FD
S_D6	\$9235F3
S_D7	\$93DBD7
S_D8	\$959267
S_D9	\$975961
S_DA	\$99307F
S_DB	\$9B1777
S_DC	\$9D0DFE
S_DD	\$9F13C8
S_DE	\$A12883
S_DF	\$A34BDF
S_E0	\$A57D86
S_E1	\$A7BD23
S_E2	\$AA0A5B
S_E3	\$AC64D5
S_E4	\$AECC33
S_E5	\$B14017
S_E6	\$B3C020
S_E7	\$B64BEB
S_E8	\$B8E313
S_E9	\$BB8533
S_EA	\$BE31E2

MOTOROLA B-5

 Table B-1
 Sine Table (continued)

ADDRESS	VALUE
S_EB	\$C0E8B6
S_EC	\$C3A946
S_ED	\$C67323
S_EE	\$C945E0
S_EF	\$CC210D
S_F0	\$CF043B
S_F1	\$D1EEF6
S_F2	\$D4E0CB
S_F3	\$D7D947
S_F4	\$DAD7F4
S_F5	\$DDDC5B
S_F6	\$E0E607
S_F7	\$E3F47E
S_F8	\$E70748
S_F9	\$EA1DEC
S_FA	\$ED37F0
S_FB	\$F054D9
S_FC	\$F3742D
S_FD	\$F69570
S_FE	\$F9B827
S_FF	\$FCDBD5

B-6 MOTOROLA

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